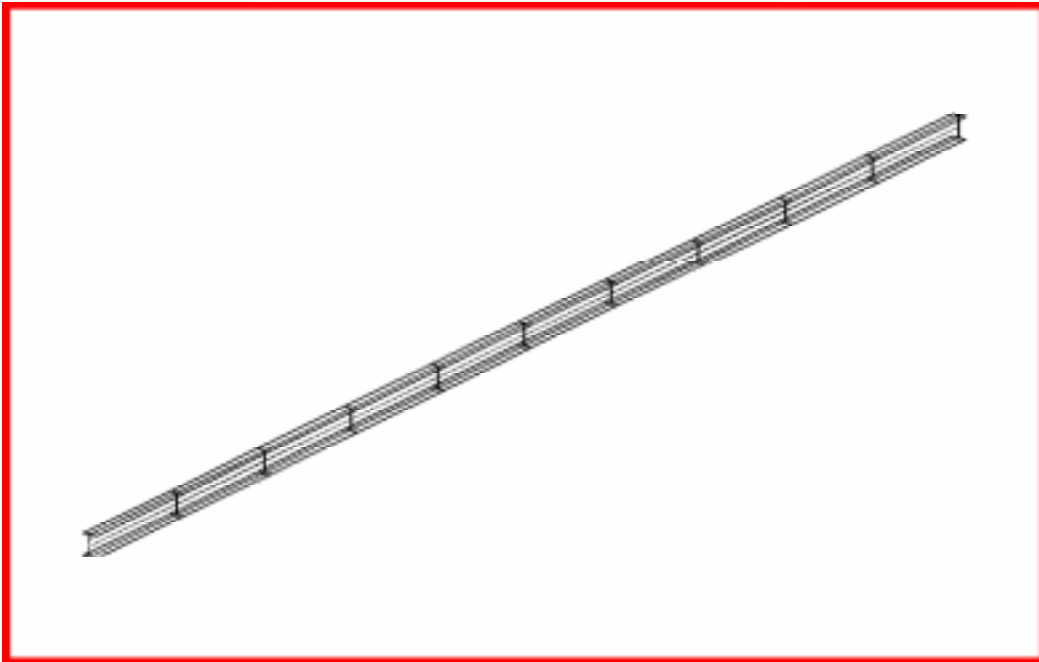


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APPENDIX B

*Normal Modes with  
Differential Stiffness  
(SI Units)*



**Objectives**

- Analyze a stiffened beam for normal modes.
- Produce NASTRAN input file that represent beam and load.
- Submit for analysis.
- Find normal modes (natural frequencies).



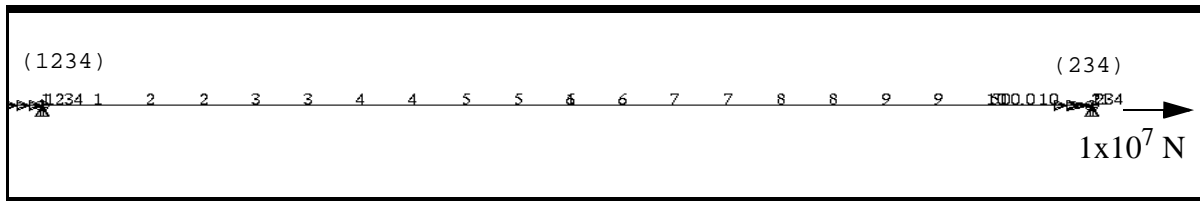
## Model Description:

The goal of this example is to analyze a stiffened model. In this case, the beam from Appendix A. with a  $1 \times 10^7$  N force applied.

Figure A-b.1 below is a finite element representation of the beam. One end is pinned in 3 translations and one rotation. The other is pinned in 2 translations and one rotation with a  $1 \times 10^7$  N force applied.

**Figure A-b.1**

Grid Coordinates and Element Connectivities



---

**Table A-b.1**

<b>Length</b>	<b><math>1.0 \times 10^3</math> mm</b>
<b>Elastic Modulus</b>	<b><math>2.0684 \times 10^5</math> MPa</b>
<b>Density</b>	<b><math>7.8334 \times 10^{-9}</math> N-sec<sup>2</sup>/mm<sup>4</sup></b>
<b>Poisson's Ratio</b>	<b>0.32</b>
<b>Area</b>	<b><math>5 \times 10^3</math> mm<sup>2</sup></b>
<b>I<sub>1</sub></b>	<b><math>1.0417 \times 10^6</math> mm<sup>4</sup></b>
<b>Force</b>	<b><math>1 \times 10^7</math> N</b>

Theoretical Solution

$$f_n = \frac{K_n}{2\pi} \left[ \frac{EIg}{Wl^4} \left( 1 + \frac{1}{Kr} \frac{Pl^2}{EI} \right) \right]^{1/2}$$

For Mode 1,  $K_r = 9.87$

$$f_n = \frac{9.87}{2\pi} \left[ \frac{(2.0684 \times 10^5)(1.0417 \times 10^6)}{(7.8334 \times 10^{-9})(5 \times 10^3)(1.0 \times 10^3)^4} \left( 1 + \frac{1}{9.87} \frac{(1 \times 10^7)(1 \times 10^3)^2}{(2.0684 \times 10^5)(1.0417 \times 10^6)} \right) \right]^{1/2}$$

$$f_n = 278.22 \text{ Hz}$$

For Static Load

$$\Delta = \frac{PL}{AE}$$

$$\Delta = \frac{(1 \times 10^7)(1 \times 10^3)}{(5 \times 10^3)(2.0684 \times 10^5)}$$

$$\Delta = 9.67 \text{ mm}$$

---

## Exercise Procedure:

1. Start up MSC.Nastran for Windows 3.0 and begin to create a new model.

Double click on the icon labeled MSC.Nastran for Windows V3.0.

On the *Open Model File* form, select **New Model**.

*Open Model File:*

**New Model**

2. Import **prob1.DAT**.

**File/Import/Analysis Model...**

**Nastran**

**MSC/Nastran**

**OK**

Change the directory to **C : \temp**.

*File name:*

**appenA.DAT**

**Open**

To reset the display of the model do the following:

**View/Redraw**

**View/Autoscale**

**OK**

3. Create the load set.

**Model/Load/Set...**

*Title:*

**pull**

**OK**

4. Define the options for a nonlinear analysis.

**Model/Load/Nonlinear Analysis...**

*Solution Type:*

**Static**

**Defaults...**

**APPENDIX B** *Normal Modes with Differential Stiffness (SI Units)*

Basic/Number of Increments:

5. Create the point loads.

**Model/Load/Nodal...**

Select **Node 11**.

(highlight)

*FX*

6. Submit the job for analysis.

**File/Export/Analysis Model...**

Analysis Type:

Change the directory to **C:\temp**.

File name:

Run Analysis

Problem ID:

Under *Output Requests*, unselect everything except:

Displacement

---

Also, change output to:

<b>Type Input...</b>	<b>2..Print and PostProcess</b>
<i>Current Line:</i>	<b>METHOD = 10</b>
<b>OK</b>	
<b>OK</b>	
<b>Type Input...</b>	
<i>Current Line:</i>	<b>PARAM, NMLOOP, 5</b>
<b>More</b>	
<i>Current Line:</i>	<b>EIGRL, 10, , , 3</b>
<b>More</b>	
<i>Current Line:</i>	<b>PARAM, COUPMASS, 1</b>
<b>OK</b>	
<b>OK</b>	

When asked if you wish to save the model, respond **Yes**.

<b>Yes</b>	
<i>File name:</i>	<b>appenB</b>
<b>Save</b>	

When the MSC.Nastran manager is through running, MSC.Nastran will be restored on your screen, and the *Message Review* form will appear. To read the messages, you could select **Show Details**. Since the analysis ran smoothly, we will not bother with the details this time.

<b>Continue</b>
-----------------

When asked if it is “OK to Begin Reading File C:\TEMP\appenB.xdb”, respond **Yes**.

<b>Yes</b>
------------

7. Determine the results of the analysis.

To list the results, select the following:

**List/Output/Query...**

Under *the Output Set* pull down menu, what are the three modes?

Note: Check the second set of modes. The first set is the results from the previous exercise.

1st = \_\_\_\_\_ Hz

2nd = \_\_\_\_\_ Hz

3rd = \_\_\_\_\_ Hz

Next, to list the displacement results, select the following:

<i>Output Set:</i>	<input type="text" value="8..Case 1 Step 1.000000"/>
<i>Category:</i>	<input type="text" value="1..Displacement"/>
<i>Entity:</i>	<input checked="" type="radio"/> Node
<i>ID:</i>	<input type="text" value="11"/>
<input type="text" value="OK"/>	

What is the total displacement?

Displacement = \_\_\_\_\_

The answer is listed at the end of the exercise. Are the answers consistent with the theoretical solutions?

When finished, exit MSC.Nastran for Windows.

**File/Exit**

This concludes this exercise.

<i>Mode 1</i>	<b>278.22 Hz</b>
<i>Mode 2</i>	<b>687.43 Hz</b>
<i>Mode 3</i>	<b>1284.67 Hz</b>
<i>Displacement</i>	<b>9.67 mm</b>

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